Module 2 :

Deep Networks

Deep Forward Networks



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Bibliography

- Deep Learning book (Goodfellow, Bengio, Courville)
- Machine Learning @ Stanford (Prof Andrew Ng)
- Hands-On Machine Learning with Scikit-Learn & Tensorflow (Aurélien Géron)





Learning Objectives

- What are Deep Forward Networks ?
- Regularization for deep learning
- Training and optimization for deep models



Deep Learning

- Definition
- Motivations
- Comparison with Machine Learning

Ability of a machine to act in a way that imitates intelligent human behaviour \

Study of the algorithms and methods that enable computers to solve specific tasks without being explicitly instructed how to solve these tasks



Subset of ML algorithms that make use of large arrays of Artificial Neural Networks

- Multiple levels of features represented by multiple layers
- Each level represents abstract features that are discovered from the features represented in the previous level.
 - level of abstraction increases with each level

Deep Learning: Definition



Machine Learning











- How do we get AI ?
 - Knowledge \rightarrow Learning
 - Generalization
 - Fight the curse of dimensionality



Deep Learning: Motivations

- 3 key ingredients for ML towards AI :
 - Lots of data
 - Very flexible models (as we get more data)
 - we change the number of hidden units
 - Powerful priors to defeat curse of dimensionality
 - 1) distributed representations
 - 2) deep architecture

 Possible to represent an exponential number of regions with a linear number of parameters

- 1. Distributed Representations
- Can learn a very complicated function with a low number of examples
- Features are individually meaningful
- 553
- Algorithms using nondistributed representations ?





- Universal approximation property (shallow NN sufficient to represent any function with required degree of accuracy)
- Deep network allows to represent the same function with fewer hidden units.
- Number of units needed in a shallow network can be <u>exponentially larger</u> than in deep enough network

Does depth imply to have a flexible family of functions ?



2. Deep

Architecture

Do deeper networks correspond to a higher capacity ?

Does deeper mean that we can represent more functions ?



input layer X hidden layer H_2 hidden layer H_1 (including activation (including activation function) function) W_1 W_2 W_3 output layer Y x_{o} net₀ y_0 x_1 Softmax net₁ y_1 x_2 net₉ y_9 (X₇₈₃₎ +1 +1 +1 b_1 b_3

Example : MNIST



• Form a basis for many commercial applications

1) CNNs are a special kind of FNN

- Used to recognize objects from photos,...

Importance of Deep Nets

- 2) They are a conceptual stepping stone to RNNs
 - Power many Natural Language Processing (NLP) applications



	Criteria	Machine Learning	Deep Learning
	Data size		
	Computer		
DL versus ML	infrastructure		
	Feature engineering		
	Nature of problem		

• Similar to linear model

- Basics of gradient descent :
 - Optimizer
 - Cost function
 - Form of output units

Design Decisions

• Unique to DFNN

- Concept of hidden layer
 - Activation functions

• Architecture of network

- Number of layers
- How they are connected to each other
- Number of units in each layer
- Learning requires gradients of complicated functions
 - Backpropagation

Training Challenges • Example : 10 layers with 100s of neurons each, connected by hundreds of thousands of connections

• Vanishing/exploding gradient problem

- Problem affecting deep neural networks
- Makes lower layers very hard to train
- Training would be extremely slow with such a large network
- Model with millions of parameters would severely risk overfitting the training set



Vanishing/ Exploding gradient problem

Exploding gradient problem (mostly in RNNs) :

- Gradients grow bigger and bigger
- Many layers get insanely large weight updates
- The algorithm diverges

Vanishing gradient problem :

- Gradients often get smaller and smaller as the algorithm progresses down to the lower layers
- Gradient Descent update leaves the lower layer connection weights virtually unchanged (training never converges to a good solution)

- Problem found to be a combination of logistic sigmoid activation functions with random initialization of the weights
 - Prefer ELU or any variant of ReLU activation functions



• Use another weight initialization (see next slide)

Solution to the Gradient Problem Weight Initialization

- The initial parameters need to break the symmetry between different units
- Use Xavier weights, the best ones to prevent gradient problems from happening: random draws from truncated normal distribution with :

$$\mu = 0$$
 and $\sigma = \sqrt{\frac{2}{a+b}}$

 Another strategy is to initialize weights by transfering weights learnt via an unsupervised learning method (method also called fine-tuning)



• Tackles the vanishing/exploding gradient problems

Input: Values of x over a mini-batch: $\mathcal{B} = \{x_{1...m}\}$; Parameters to be learned: γ , β **Output:** $\{y_i = BN_{\gamma,\beta}(x_i)\}$ $\mu_{\mathcal{B}} \leftarrow \frac{1}{m} \sum_{i=1}^{m} x_i$ // mini-batch mean $\sigma_{\mathcal{B}}^2 \leftarrow \frac{1}{m} \sum_{i=1}^m (x_i - \mu_{\mathcal{B}})^2$ // mini-batch variance $\widehat{x}_i \leftarrow \frac{x_i - \mu \beta}{\sqrt{\sigma_R^2 + \epsilon}}$ // normalize $y_i \leftarrow \gamma \hat{x}_i + \beta \equiv \mathbf{BN}_{\gamma,\beta}(x_i)$ // scale and shift

Add an operation in the model just before the activation function of each layer to zero-center and normalize inputs:mean/std evaluation using the current mini-batch Scale and shift the result using two

parameters per layer

 \checkmark

Batch

Normalization

Networks much less sensitive to weight initialization

Possible to use much larger learning rates

Gradient Clipping

- Tackles the exploding gradient problem
- Clip the gradient during backpropagation so that they never exceed some threshold

• Mostly used in RNNs

- Nowadays, people prefer batch normalization
 - gradient clipping not ideal because of loss of information

 Always try to find an existing neural network that accomplishes a similar task to the one you are trying to tackle

Reusing Pretrained Layers • Transfer Learning : reuse the lower layers of this network

• Output layer should usually be replaced

• Speeds up training and requires much fewer training data



Pre-training : training on cat images Fine-tuning : update the weights for radiology Summary of techniques to speed up training • Good initialization strategy for the connection weights (Xavier)

- Good activation function (ReLU, ELU)
- Batch Normalization
- Reusing parts of a pretrained network (transfer learning)
- Faster optimizer (momentum, Adam)

Initialization	He initialization			
Activation function	ELU			
Normalization	Batch normalization			
Regularization	Dropout			
Optimizer	Gradient Descent			
Learning rate schedule	None			

• What can you try if :

• You can't find a good learning rate ?

• Your training set is too small ?

• You need a lightning-fast model at runtime ?

Exercise





Two-Minute Papers



Optimization

In terms of performance and time

1. Performance

Bias reduction techniques Variance reduction techniques





- Bayes optimal error
- Human-level error
- Training error
- Dev error

- Test error
- Real world

Avoidable bias

Variance

Depending on where you get the *largest discrepancy*, you will use a different technique to tackle the problem

	Bias reduction technique		Variance reduction technique		
	Development error	6		5	0.8
	Training error	5		1	0.7
		0.5		0.5	
List of Errors	Human (proxy for Bayes error)	0.7		0.7	0.5
		1		1	
	classification	Scenario A		Scenario B	Scenario C
	Medical image	Classification error (%)			



Bias Reduction techniques

Hyperparameter tuning Model tuning Optimization algorithm



• To go deeper helps generalization



better to have many simple layers than few highly complex ones Hyperparameters: number of neurons in hidden layers

- Input and output layer number of neurons is determined by the type of input/output of the task
- For hidden layers, common practice was historically to size them to form a funnel, with fewer neurons at each layer
- Now, simply use the same size for all hidden layers
 - Only one hyperparameter left

A generalisation of ReLU is

 $g(z,\alpha)=\max\{0,z\}+\alpha\min\{0,z\}$

To avoid a null gradient the following are in use

1. Absolute value rectification $\alpha = -1$

- 2. Leaky ReLU
- 3. Parametric ReLU
- 4. Maxout Units

 $\alpha = 0.01$

 α learnable

$$g(z)_i = \max_{j \in S_i} z_j$$
$$\cup_i S_i = [1, \dots, m]$$
$$S_i \cap S_j = \emptyset \quad i \neq j$$

Hyperparameters: activation function

Hyperparameters: global search



Grid Search



Random Search



Adaptive Selection



Unimportant parameter

Grid Layout



Random Layout



Important parameter

<u>Demo</u>





 chosen such that they have a non-flat region when the answer is incorrect

• Exponential or logarithm functions help

Model: loss function

- Other functions : • $L_1(\hat{y}, y) = \sum_{i=0}^m |y^i - \hat{y}^i|$ (L1 loss) • $L_1(\hat{y}, y) = \sum_{i=0}^m (y^i - \hat{y}^i)^2$ (L2 loss)
 - $L_2(\hat{y}, y) = \sum_{i=0}^m (y^i \hat{y}^i)^2$ (L2 loss) • ...



DARTS: DIFFERENTIABLE ARCHITECTURE SEARCH

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ABSTRACT

This paper addresses the scalability challenge of architecture search by formulating the task in a differentiable manner. Unlike conventional approaches of applying evolution or reinforcement learning over a discrete and non-differentiable search space, our method is based on the continuous relaxation of the architecture representation, allowing efficient search of the architecture using gradient descent. Extensive experiments on CIFAR-10, ImageNet, Penn Treebank and WikiText-2 show that our algorithm excels in discovering high-performance convolutional architectures for image classification and recurrent architectures for language modeling, while being orders of magnitude faster than state-of-the-art non-differentiable techniques. Our implementation has been made publicly available to facilitate further research on efficient architecture search algorithms.



Model: global architecture

Optimization Algorithm (*Reminder*)







Two-Minute Papers

Variance Reduction techniques

Bigger training set Regularization





• Different strategies :

1) Dataset (division, augmentation,...)

2) Model (dropout, L2 regularization,...)

3) Training (early stopping)

 Use cases : if few data or if model has more than 50 layers (CNN) 1. Regularization (dataset): Division • Divide the data into a training, validation and test sets

- Training set to define the optimal predictor
- Validation set to choose the capacity
- Test set to evaluate the performance



• Apply realistic transformations to data to create new synthetic samples, with same label

affine elastic distortion deformation noise original hue shift horizontal random flip translation

• Process also called jittering

1. Regularization

(dataset):

Augmentation

• Labels might be wrong (human annotation)

 Instead of asking the model to predict 1 for the right class, we ask it to predict 1-ε for the correct class and ε for all the others

$$ext{cross-entropy loss} = (1-\epsilon) \mathit{ce}(i) + \epsilon \sum rac{\mathit{ce}(j)}{N}$$

 Regularization (dataset): Label Smoothing • Apply it both in forward and backward propagations

BUT use it only in the training phase !



2. Regularization (model): Dropout





TWO MINUTE PAPERS

TRAINING DEEP NEURAL NETWORKS WITH DROPOUT

Disclaimer: I was not part of this research project, I am merely providing commentary on this work.

Two-Minute Papers

• Modify the cost function (add soft constraint) :

Regularization

(model):

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$$J = -\frac{1}{m} \sum_{i=1}^{m} \left(y^{(i)} \log \left(a^{[L](i)} \right) + (1 - y^{(i)}) \log \left(1 - a^{[L](i)} \right) \right)$$

$$J_{regularized} = -\frac{1}{m} \sum_{i=1}^{m} \left(y^{(i)} \log \left(a^{[L](i)} \right) + (1 - y^{(i)}) \log \left(1 - a^{[L](i)} \right) \right) + \underbrace{\frac{1}{m} \frac{\lambda}{2}}_{L2 \text{ regularization cost}} \sum_{L2 \text{ regularization cost}} W_{k,j}^{[I]2}$$

 λ regulates the complexity/capacity of the predictors. It smoothens the decision boundary → weights pushed to smaller values.

- Typical values : logarithmic scale between 0 and 0.1, such as 0.1, 0.001, 0.0001 (tuned using dev set)
 - If λ is too large, it can "oversmooth", resulting in a model with high bias³



• Stop training before the validation set error start growing



2. Time

How to improve time consumption when critical to get results

Material Acceleration (GPUs)

END-TO-END PRODUCT FAMILY



Material Acceleration : Example

TESLA PLATFORM ENABLES DRAMATIC REDUCTION IN TIME TO TRAIN



Relative Time to Train Improvements



https://b.socrative.com/login/student/

Room : CONTI6128